## Exam. Code : 209001 Subject Code : 3751

### M.Sc. Physics 1<sup>st</sup> Semester PHY-402 : MATHEMATICAL PHYSICS

Time Allowed—3 Hours] [Maximum Marks—100 **Note** :— The question paper has *four* Sections (A-D). Attempt *five* questions selecting at least *one* question from each section. The fifth question may be attempted from any section.

#### SECTION-A

1. (a) Plot graph of the following function :  $f(x) = x \quad 0 \le x \le 4$ 

= -x, -4 < x < 0, period of function = 8

- (b) Develop the Fourier cosine expansion of f(x) = -x in the half interval (0, L).
- (c) Find the Fourier transform of

$$f(x) = 1/\epsilon |x| < 1$$

$$= 0 |\mathbf{x}| > 1$$
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2. (a) Define symmetric, anti-symmetric and mixed tensors. 5

- (b) Find the expression of a curl of a vector function in cylindrical co-ordinates. 10
- (c) By use of summation convention rewrite :

$$d\phi = \frac{\partial \phi}{\partial x} dx + \frac{\partial \phi}{\partial y} dy + \frac{\partial \phi}{\partial z} dz$$

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1

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#### SECTION-B

3. (a) Using Frobenius method solve the differential equation :

$$x^{2}\frac{d^{2}y}{dx^{2}} + 6x\frac{dy}{dx} + (6 - x^{2})y = 0.$$
 10

(b) Write down the expression for generating function of Bessel function, J<sub>n</sub>(x). Use it to prove that :

 $\frac{d}{dx}(J_n(x)) = \frac{1}{2}(J_{n-1}(x) + J_{n+1}(x))$  for the case of integer, n. 10

- 4. (a) Consider the Laplace equation Δ<sup>2</sup>u = 0 in spherical coordinates, assume u = RΘ, where R depends only on r and Θ only on θ, use the method of separation of variables to obtain two equations only in r and θ variables. What are the solutions of equation of R known as ? 12
  - (b) Define Gamma function,  $\Gamma(n)$ , show that :

$$1.3.5.7....(2n-1) = \frac{2^{1-n}\Gamma(2n)}{\Gamma(n)}$$

### SECTION-C

5. (a) State the prove Cauchy residue theorem. 10

- (b) Classify the singularities and calculate the residue for F(z) = z.exp(1/z).
- (c) By use of the residue theorem, evaluate :

$$\int_{0}^{2\pi} \frac{d\vartheta}{3 - 2\cos\vartheta + \sin\vartheta}$$

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5. (a) Show that 
$$\int_{z_0}^{z} Z^n dz = \frac{Z^{n+1} - Z_0^{n+1}}{n+1}$$

for all n, except n = -1. Discuss the case for n = -1. 10

(b) By use of residue theorem, evaluate :

$$I = \int_{-\infty}^{\infty} \frac{\sin x}{x} dx$$
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(c) Find the Laurent expansion for  $F(Z) = \frac{1}{Z(Z-2)}$ in the region 0 < |z| < 2.

### SECTION-D

- 7. (a) Show that the following sets are groups under the given laws of composition :
  - (i) The set of all m×n matrices under matrix addition.
  - (ii) The set of all non-zero rational numbers under scalar multiplication.
  - (b) Define permutation group and give one example.
    Discuss their importance in quantum mechanics of identical particles.
    10

2367(2118)/DAG-12289 3 (Contd.)

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- 8. (a) Explain what is Isomorphism and Homomorphism.
  - (b) Consider the following four operations in the XY plane :

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- (i) No change  $\{x \to x, y \to y\}$
- (ii) Inversion  $\{x \rightarrow -x, y \rightarrow -y\}$
- (iii) Reflection  $\{x \rightarrow -x, y \rightarrow y\}$ 
  - (iv) Reflection  $\{x \rightarrow x, y \rightarrow -y\}$

Prove that these four operations form a mathematical group. 10

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